# Mechanism of Substrate Translocation by a Ring-Shaped ATPase Motor at Millisecond Resolution 

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S Supporting Information


#### Abstract

Ring-shaped, hexameric ATPase motors fulfill key functions in cellular processes, such as genome replication, transcription, or protein degradation, by translocating a long substrate through their central pore powered by ATP hydrolysis. Despite intense research efforts, the atomic-level mechanism transmitting chemical energy from hydrolysis into mechanical force that translocates the substrate is still unclear. Here we employ all-atom molecular dynamics simulations combined with advanced path sampling techniques and milestoning analysis to characterize how mRNA substrate is  translocated by an exemplary homohexameric motor, the transcription termination factor Rho. We find that the release of hydrolysis product ( $\mathrm{ADP}+\mathrm{Pi}$ ) triggers the force-generating process of Rho through a 0.1 millisecond-long conformational transition, the time scale seen also in experiment. The calculated free energy profiles and kinetics show that Rho unidirectionally translocates the single-stranded RNA substrate via a population shift of the conformational states of Rho; upon hydrolysis product release, the most favorable conformation shifts from the pretranslocation state to the post-translocation state. Via two previously unidentified intermediate states, the RNA chain is seen to be pulled by six K326 side chains, whose motions are induced by highly coordinated relative translation and rotation of Rho's six subunits. The present study not only reveals in new detail the mechanism employed by ring-shaped ATPase motors, for example the use of loosely bound and tightly bound hydrolysis reactant and product states to coordinate motor action, but also provides an effective approach to identify allosteric sites of multimeric enzymes in general.


## INTRODUCTION

One of the most remarkable inventions of biological evolution is molecular motors driven by energy released from ATP hydrolysis. Among such motors, ring-shaped, hexameric motors participate in many vital processes, such as DNA replication, transcription, chromosome segregation, protein degradation, and maintenance of pH homeostasis; ${ }^{1,2}$ most of these hexameric motors belong to the so-called additional strand catalytic glutamate (ASCE) superfamily of proteins. ${ }^{1}$ Emerging evidence shows that a number of these hexameric motors can be targets for cancer therapy. ${ }^{3-6}$ Characterizing the atomic level mechanism of their function on a biologically relevant time scale (millisecond or longer) could aid the development of anticancer drug design. ${ }^{7}$

The function of the ring-shaped motors is carried out in a series of repeated steps, by generating linear force or torque on the substrate (nucleic acid strand, polypeptide, or central stalk) inside the central pore of the ring. Each step of the motors contains, according to single-molecule observation, a dwell phase of relative long duration and a motor-action phase. ${ }^{2}$ During the dwell phase, the motor is energetically charged through the occurrence of three chemical processes, namely (1) ATP binding, (2) release of existing (i.e., "old") ATP hydrolysis product, and (3) hydrolysis of ATP into "new" product, before
the next motor-action phase takes place. This scenario is illustrated schematically in Figure S1 in Supporting Information. Interestingly, none of the three chemical processes during the dwell phase are directly involved in mechanical force generation since these processes happen at subunit-subunit interfaces along the ring, distant from the substrate binding site inside the central pore where mechanical force is actually being applied. The question addressed in the present study is how the free energy stored in the motor during the dwell phase is transferred to power substrate motion in the motor-action phase.

Crystal structures of hexameric helicases ${ }^{8-10}$ and $\mathrm{F}_{1}-/ \mathrm{V}_{1^{-}}$ ATPase ${ }^{11,12}$ with substrates and ligands (ATP-mimic molecules) bound provide evidence that large-scale conformational transitions are responsible for the substrate movement. In the present study we focus on an exemplary homohexameric helicase, Rho, whose equilibrium structure in complex with its RNA substrate and ligands (ATP analogue $\mathrm{ADP} \cdot \mathrm{BeF}_{3}$ ) has been solved. ${ }^{9}$ Rho is a key factor in bacterial gene expression and regulation, ${ }^{13}$ with a primary role in transcription termination through translocating the nascent mRNA in the

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Figure 1. Structure and proposed rotary reaction mechanism of Rho hexameric helicase. (a) Structure modeled based on the reported Rho crystal structure (pdb code: 3ICE). ${ }^{9}$ Rho subunits consist of a C-terminal domain (blue) and an N-terminal domain (gray). Active sites of the ATPase cycle are located at the subunit-subunit interfaces and are labeled according to the state of ATP at the respective sites, namely, hydrolysis-competent (T*), ATP-bound (T), "old" product (D), and empty (E) state, respectively. ATP, ADP, and Pi are shown in orange. K326 residues (purple), contributed by each subunit and altogether arranged in a roughly helical stair case fashion, are located in the central channel of the Rho hexamer where RNA (pale red) is bound, likewise in a roughly helical conformation. (b) Proposed rotary reaction mechanism. ${ }^{9}$ Rho's six identical subunits are labeled $m_{1}, m_{2}, \ldots, m_{6}$; the different colors of the six subunits' circular peripheries indicate schematically that the subunits assume different interface conformations in prior state R . In binding ATP, releasing ADP + Pi and hydrolyzing ATP to ADP, the pattern of ligand binding states corresponding to the surface conformations in the prior state $\mathrm{R}, \mathrm{T} * \mathrm{~T} * \mathrm{TTED}$, shifts to $\mathrm{DT} * \mathrm{~T} * \mathrm{TTE}$ in the final state F . As one can easily recognize, the ligand binding states of R, after a $60^{\circ}$ clockwise rotation around the $z$-axis, are the same as those of F . In going from R to F , RNA is propelled as indicated by pale (RNA further away from viewer) and intense red (RNA closer to viewer) coloration.
$5^{\prime} \rightarrow 3^{\prime}$ direction and terminating transcription upon reaching the RNA polymerase. ${ }^{14-16}$ The asymmetric structure of Rho ${ }^{9}$ reveals that the six interfaces between Rho's six subunits exhibit a specific circular pattern of different conformational states in the ATP hydrolysis cycle, the states being related to six sequential ligand binding states $\mathrm{T}^{*}, \mathrm{~T}^{*}, \mathrm{~T}, \mathrm{~T}, \mathrm{E}, \mathrm{D}$ shown and defined in Figure 1a. According to the crystal structure, Rho translocation, driven by ATP binding, hydrolysis, and product release processes, should involve rotary reaction steps (Figure 1b). In each step the mentioned circular conformational pattern is shifted by one subunit or, rather, by $60^{\circ}$ around the Rho ring. Such a rotary reaction mechanism, postulated originally by Boyer for $\mathrm{F}_{1}$-ATPase, ${ }^{17}$ has also been suggested, based on crystal structures, for other hexameric helicases ${ }^{8,10}$ and $\mathrm{F}_{1^{-}} / \mathrm{V}_{1^{-}}$ ATPase, ${ }^{11,12}$ the latter of which share considerable sequence and structural similarities with Rho. ${ }^{18}$

Despite the valuable information provided by the crystal structure, ${ }^{9}$ various biochemistry experiments ${ }^{19-21}$ and a singlemolecule study ${ }^{22}$ on Rho, the following three questions remain unanswered: (1) The rate-limiting step in the Rho hydrolysis cycle, the latter combining dwell phase and motor-action phase, seems to be release of "old" hydrolysis product as suggested by experiments, ${ }^{19,20}$ but whether and how this product release triggers the ring to exert force on the RNA substrate is unknown. (2) A specific direction (clockwise in the case of Rho) of the rotary reaction steps, along with an asymmetry pattern of the ring subunits interacting with the substrate, ${ }^{23}$ is required for the substrate's unidirectional translocation. ${ }^{1}$ How is the direction of the rotary reaction step selected and
maintained, or how far is the transition involved in Rho's motor-action phase (Figure lb) energetically favorable? (3) What conformational transition arises at the "new" product binding site such that "new" product turns into "old" product and can be released.

Previous computational studies on ring-shaped motors have shed light on the coupling between substrate dynamics and coordinated subunit conformational transition during the ATP hydrolysis cycle; however, the studies included only coarsegrained simulations ${ }^{24-27}$ or enforced rotation simulations of the central stalk in the all-atomic $\mathrm{F}_{1}$-ATPase system; ${ }^{28-30}$ furthermore, the studies could not answer the above questions due to model resolution or time scale limitations. Today allatom molecular dynamics (MD) simulations can achieve very large and very long simulations of protein dynamics, as reported recently in the cases of HIV capsid assembly ${ }^{31}$ and protein folding. ${ }^{32}$ However, due to the millisecond scale of the Rho conformational transition along with Rho's large size, straightforward MD simulations cannot reach the time scale of the transitions. Fortunately, transition pathway techniques for sampling rare transition events in protein conformational dynamics ${ }^{33,34}$ can be utilized to overcome the time scale challenge; here we carry out MD simulations employing the string method ${ }^{7,35}$ and the milestoning technique ${ }^{36-39}$ to characterize the conformational transition pathway of Rho's action phase along with associated free energy profile and kinetic rates in the Rho-RNA complex.

The transition pathway determined at atomic resolution reveals the relative translation and rotation of the six subunits
that unidirectionally translocate RNA. The six-subunit motion induces RNA translocation mainly through six lysine residues arranged in the pore along a spiral staircase, one (K326) contributed by each subunit. We find that, during one rotary reaction step, the force generation process is induced by release of "old", actually loosely bound, product and eventually leads to one K326 residue (belonging to subunit $m_{1}$ in Figure 1b), namely the one at the top of the staircase, being pulled away from the RNA substrate, while the interactions between the second- and third-to-top K326 residues with RNA are firmly held. The disengagement between the top K326 and RNA exhibits the slowest $\sim 0.1 \mathrm{~ms}$ transition between two key intermediate states. The directionality of the rotary reaction in Rho's action phase, which starts upon completion of the three ligand state changes during the dwell phase, is induced by a 1.5 $\mathrm{kcal} / \mathrm{mol}$ drop in free energy between pretranslocation and post-translocation states, suggesting a population shift mechanism for the force generation. Furthermore, among functionally important residues identified, a small subset of residues is found to form an allosteric pathway that couples unbinding of K326 from RNA with product release; this allosteric regulation changes a tight binding of the "new" hydrolysis product into a loose binding, so that the product changes its characteristic to that of "old" product that can be released in the subsequent dwell phase initiating the next motor-action phase.

## RESULTS

In the following the basic rotary reaction step from prior state R to final state F, as defined in Figure 1b, is described in detail. We first characterize the millisecond-scale conformational transition of the Rho-RNA complex along with the associated free energy profiles and kinetics. We then show in atomic level detail the relative motion of the six subunits, in particular the motion of the six lysines K326, and demonstrate how these motions unidirectionally translocate RNA. Finally, based on the transition pathway, we identify residues involved in an essential allosteric control pathway that synchronizes RNA translocation and the ATP hydrolysis cycle.

Thermodynamics and Kinetics of a Basic Rotary Reaction Step. The rotary reaction $\mathrm{R} \rightarrow \mathrm{F}$ (Figures 1 b and 2a) is driven by ligand state changes of the ATP hydrolysis cycle. The state R represents a stable state corresponding to the crystal structure; in this state Rho does not transition spontaneously to F . Three subprocesses occurring during Rho's dwell phase (see Figure S1) are required to bring about a motor-action phase transition toward F: (1) binding of ATP to the empty site, namely $\mathrm{E} \rightarrow \mathrm{T}$; (2) release of "old" hydrolysis product ( $\mathrm{ADP}+\mathrm{Pi}$ ), namely $\mathrm{D} \rightarrow \mathrm{E}$; (3) formation of "new" hydrolysis product through the reaction ATP $\rightarrow \mathrm{ADP}+\mathrm{Pi}$, namely $\mathrm{T}^{*} \rightarrow \mathrm{D}^{*}$. D represents here a state of loosely bound ("old") product and $\mathrm{D}^{*}$ a state of tightly bound ("new") product.

The subprocesses $(1,2,3)$ take place somewhere along the transition $\mathrm{R} \rightarrow \mathrm{F}$. Based on experimental studies, ${ }^{19,20}$ subprocess (2) is considered rate limiting. Accordingly, we assume in our study that subprocesses $(1,3)$ take place at the very beginning of the $\mathrm{R} \rightarrow \mathrm{F}$ transition; to elucidate the ratelimiting nature of subprocess (2) we introduce at the $m_{6} / m_{1}$ interface a ligand state $\mathrm{X}=\mathrm{E}$ or D that we choose to have, respectively, product released right away or not released at all. The transition modeled by us is then actually $\mathrm{R} \rightarrow \mathrm{I} \rightarrow \mathrm{F}$, where $I$ is introduced and shown in Figure 2a; I differs from R by the change in ligand configuration $\mathrm{T}^{*}, \mathrm{~T}^{*}, \mathrm{~T}, \mathrm{~T}, \mathrm{E}, \mathrm{D}$ (state




Figure 2. Free energy profiles and mean first passage times characterizing the rotatory reaction step of Rho. (a) Rotary reaction scheme. Details of how states R, I, and F have been constructed are described in the Methods section. The ligand state X at the interface between subunits $m_{6}$ and $m_{1}$ is assumed to be in one case the empty state E and in another case the ("old") product bound state D. The free energy profiles during the transition $\mathrm{I} \rightarrow \mathrm{F}$ for cases $\mathrm{X}=\mathrm{E}$ and X $=\mathrm{D}$ are shown in (b) and (c), respectively. The standard error shown is estimated by repeating the free energy calculations with half of the trajectories. Insets in (b) and (c) show both the forward and backward mean first passage times. In case $\mathrm{X}=\mathrm{E}$ the rotary reaction is exergonic, whereas in case $\mathrm{X}=\mathrm{D}$ the rotary reaction is strongly endergonic.
R) $\rightarrow D^{*}, T^{*}, T, T, T^{-}, X$ (state I) (see Methods for details of R , I , and F modeling based on the crystal structure and biochemical measurements).

We first describe the optimal I $\rightarrow$ F pathway for the choice of $\mathrm{X}=\mathrm{E}$. As shown in Figure 2 b the reaction starts in the first local minimum at state I, and eventually, the system reaches the final state F , which is seen to lie energetically below I, namely by $\Delta G_{\mathrm{I}, \mathrm{F}}=-1.5 \mathrm{kcal} / \mathrm{mol}$; this energy drives the rotary reaction forward. The I $\rightarrow \mathrm{F}$ transition happens in three steps, namely by overcoming a barrier of height $\epsilon_{1}=1.3 \mathrm{kcal} / \mathrm{mol}$ and reaching a first intermediate IM1, by overcoming a second barrier of height $\epsilon_{2}=5.0 \mathrm{kcal} / \mathrm{mol}$ at the main transition state (TS) and reaching a second intermediate IM2, and finally by overcoming a third, small energy barrier of height $\epsilon_{3}=0.3 \mathrm{kcal} /$ mol and reaching the final state F . The conformations of the intermediates IM1 and IM2 arising in case of $\mathrm{X}=\mathrm{E}$ will be discussed further below. The calculated mean first passage time (MFPT) from I to F is evaluated to be about 0.11 ms , consistent with the experimentally estimated value shown in Table 1. The forward rate constant for the I $\rightarrow \mathrm{F}$ transition is about 15 times larger than the reverse rate constant. As listed in Table 1, the rate-limiting step for the $\mathrm{I} \rightarrow \mathrm{F}$ transition, namely the step with the highest free energy barrier, is actually the IM1 $\rightarrow$ IM2 step.
We also find the $\mathrm{I} \rightarrow \mathrm{F}$ transition pathway for the case $\mathrm{X}=\mathrm{D}$ (hydrolysis product is not released from the $m_{6} / m_{1}$ interface

Table 1. Comparison between Calculated and Experimental MFPTs

|  | $\tau_{\mathrm{I} \rightarrow \mathrm{IM} 1}$ | $\tau_{\mathrm{IM} 1 \rightarrow \mathrm{IM} 2}$ | $\tau_{\mathrm{IM} 2 \rightarrow \mathrm{~F}}$ | $\tau_{\mathrm{I} \rightarrow \mathrm{F}}$ |
| :--- | :---: | :---: | :---: | :---: |
| calculated $^{a}$ | 183 ns | $107 \mu \mathrm{~s}$ | $2.75 \mu \mathrm{~s}$ | 0.11 ms |
| experimental $^{b}$ | - | - | - | $10^{-1}$ to 1 ms (ref 19) |

${ }^{a}$ Results from the simulation for $\mathrm{X}=\mathrm{E}$. ${ }^{b}$ Experimental MFPTs for the protein conformational transitions are order of magnitude estimates as reported in the references.
binding pocket). The free energy and mean first passage times are presented in Figure 2c. A comparison of Figure 2c and 2b shows clearly that the rotary reaction proceeds much better when the product release happens early on in state I. In fact, without product release the overall reaction is strongly endergonic $\left(\Delta G_{\mathrm{I}, \mathrm{F}}=+7 \mathrm{kcal} / \mathrm{mol}\right)$, and the forward rate constant is 1000 times smaller than the reverse rate constant. The results suggest that the conformations of states I and F exist in both $\mathrm{X}=\mathrm{E}$ and $\mathrm{X}=\mathrm{D}$ situations; hydrolysis product release shifts the relative population of these conformations and makes the state F more favorable.

Relative Translation and Rotation of Six Rho Subunits Accompanied by the Opening of the Empty Interface. In the following we analyze the characteristics essential for Rho's overall motion along the transition pathway after product release. Figure 3a shows the overall translational motion of the six Rho subunits along the $z$-axis. To simplify the description, we introduced a moving coordinate system in which the $z$ coordinates of subunits $m_{3}$ and $m_{4}$ remain constant. The remaining subunits engage all into downward movement, subunits $m_{1}$ and $m_{6}$ exhibiting the most significant movement. In state I, five of the subunits ( $m_{1}, m_{2}, \ldots, m_{5}$ ) are arranged roughly like a downward staircase $\left(\mathrm{Z}\left(m_{1}\right)>\mathrm{Z}\left(m_{2}\right)>\mathrm{Z}\left(m_{3}\right)>\right.$ $\left.\mathrm{Z}\left(m_{4}\right) \sim \mathrm{Z}\left(m_{5}\right)\right)$, where $\mathrm{Z}\left(m_{i}\right)$ is the position of subunit $m_{i}$ on the $z$-axis. $m_{6}$ is the out-of-order subunit with $\mathrm{Z}\left(m_{2}\right)>\mathrm{Z}\left(m_{6}\right)>$ $\mathrm{Z}\left(m_{3}\right)$. In state F , the five subunits $\left(m_{2}, m_{3}, \ldots, m_{6}\right)$ form a downward staircase $\left(\mathrm{Z}\left(m_{2}\right)>\mathrm{Z}\left(m_{3}\right)>\mathrm{Z}\left(m_{4}\right)>\mathrm{Z}\left(m_{5}\right) \sim\right.$ $\left.\mathrm{Z}\left(m_{6}\right)\right)$ with $m_{1}$ being now the out-of-order subunit with $\mathrm{Z}\left(m_{3}\right)$ $>\mathrm{Z}\left(m_{1}\right)>\mathrm{Z}\left(m_{4}\right)$. The vertical positions of the Rho subunits in states I and F are roughly shifted counterclockwise by one subunit. Figure 3 b shows the front view of six subunits in states I and F, with $m_{6}$ moving down by $7 \AA$ and $m_{1}$ by $5 \AA$.

The release of "old" hydrolysis product (the D $\rightarrow \mathrm{E}$ subprocess) happens at the interface between $m_{6}$ and $m_{1}$ and exerts a big influence on the conformational dynamics of that interface. We monitored the two-dimensional (2D) free energy map for the contact area between $m_{6}$ and $m_{1}$ and the crossing angle between principal axes of $m_{6}$ and $m_{1}$ (Figure 3c). During the I $\rightarrow$ F transition, the $m_{6} / m_{1}$ interface (the empty interface) turns into an open binding site via the four states I, IM1, IM2, and F as described previously in Figure 2b. Interestingly, a main free energy barrier of height $4 \mathrm{kcal} / \mathrm{mol}$ is found between states IM1 and IM2 in the 2D map, indicating the opening of the $m_{6} /$ $m_{1}$ interface is a key transition event during the I $\rightarrow \mathrm{F}$ transition. Two insets in Figure 3c show that the crossing angle becomes larger as the two subunits rotate relative to each other. After product release, the empty interface can adopt either a more stable "open" conformation or a less stable "closed" conformation; ATP binding in the next rotary reaction step would shift the population toward the closed conformation. Clearly, an empty interface is essential for hexameric motor function as proposed for several systems. ${ }^{8,9,40}$


Figure 3. Relative translational and rotational motion of subunits during the $\mathrm{I} \rightarrow \mathrm{F}$ transition. (a) Projection of subunit positions (center of mass of each subunit's atoms in the collective variable set) on the $z$ axis as a function of the progress along the discrete reaction coordinate $(0,1, \ldots, 50)$, namely the image numbering representing the progress of the transition pathway. (b) Front view of the six subunits in the initial state I (left) and in the final state F (right). The motion of $m_{6}$ along the $z$-axis is indicated by a blue arrow. The subunit colors are consistent with (a). (c) 2D free energy landscape generated using the contact area between $m_{1}$ and $m_{6}\left(\sigma_{61}\right)$ and the crossing angle between the principal axes of $m_{1}$ and $m_{6}\left(\theta_{61}\right)$ as coordinates. The unit for the free energy is kcal/mol. States I, IM1, IM2, and F (as labeled in Figure 2b) are shown as black dots. Insets demonstrate the relative orientations between $m_{1}$ and $m_{6}$ in state I (bottom left inset) and in state F (top right inset).

How Unidirectional RNA Translocation Is Coupled to Rho Conformational Transitions. The coordinated motion of Rho's subunits as seen in the simulations serves the purpose of translocating the bound RNA along Rho's central pore. The translocation results from a coupling between Rho subunits and RNA, actually involving mainly interactions between six lysines K326 of subunits $m_{1}, m_{2}, \ldots, m_{6}$ and the RNA backbone. The $\mathbf{Q}$ loops of the subunits directed toward the central pore also contribute to RNA translocation, however, the contribution of the K326 side chains in translocating RNA is larger (see Figure S6a).

In the $\mathrm{I} \rightarrow \mathrm{F}$ transition, the individual subunits $m_{1}, m_{2}, \ldots, m_{6}$ play different roles. In regard to the interaction between Rho and RNA, K326 of $m_{1}$ disengages from an interaction with phosphate group $\mathrm{P}_{3}$ of the RNA backbone; K326 of $m_{4}$ engages into a new interaction with $\mathrm{P}_{6} ; \mathrm{K} 326$ of $m_{2}$ and $m_{3}$ continue their strong interaction with $\mathrm{P}_{4}$ and $\mathrm{P}_{5}$, respectively; K326 of $m_{5}$ and $m_{6}$ do not engage in significant interactions with RNA. The
placement of RNA in the Rho channel and the translocation step is illustrated in movie S1.

The above important switching of interactions between K326 and RNA backbones can be illustrated by measuring the distances between $\mathrm{P}_{3}$ and $\mathrm{K} 326\left(m_{1}\right)$ and $\mathrm{P}_{6}$ and $\mathrm{K} 326\left(m_{4}\right)$ along the transition pathway. Figure 4 a shows the 2D free


Figure 4. Key interactions between RNA and Rho during the $I \rightarrow F$ transition. (a) Free energy landscape along distances $\mathrm{P}_{3}-\mathrm{K} 326\left(m_{1}\right)$ and $\mathrm{P}_{6}-\mathrm{K} 326\left(m_{4}\right)$. The position of the phosphorus atoms of the phosphate group and NZ atoms of K326 define the corresponding distances. (b-e) Configurations in states I, IM1, IM2, and F, accounting for the key steps of RNA binding and release that induce RNA translocation. Red dashed arrows indicate large side chain movements before the next state is reached. $m_{1}$ (green) and $m_{4}$ (orange) are shown in transparent surfaces.
energy landscape generated using the distances $\mathrm{P}_{3}-\mathrm{K} 326\left(m_{1}\right)$ and $\mathrm{P}_{6}-\mathrm{K} 326\left(m_{4}\right)$. The configurations of four local minima corresponding to states I, IM1, IM2, and F are shown in Figure $4 \mathrm{~b}-\mathrm{e}$. During the I $\rightarrow$ IM1 stage, $\mathrm{K} 326\left(m_{1}\right)$ first breaks its contact with $\mathrm{P}_{3}$, after which $\mathrm{K} 326\left(m_{4}\right)$ reduces its distance to $\mathrm{P}_{6}$ by $4 \AA$ but does not engage yet with $\mathrm{P}_{6}$. In the state IM1, $\mathrm{K} 326\left(m_{1}\right)$ forms contact with RNA base $\mathrm{U}_{6}$ (Figure 4c), indicating a different RNA sequence could give a different free energy profile. During the IM1 $\rightarrow$ IM2 transition, the distance between $\mathrm{P}_{3}$ and $\mathrm{K} 326\left(m_{1}\right)$ gradually increases at which point K326 $\left(m_{1}\right)$ loses all contact with RNA. During the last, IM2 $\rightarrow$ F, transition, K326 $\left(m_{4}\right)$ eventually coordinates with RNA phosphate $\mathrm{P}_{6}$. Since crossing of the TS happens during the IM1 $\rightarrow$ IM2 transition, the disassociation of RNA from K326 $\left(m_{1}\right)$ rather than the association of RNA with $\mathrm{K} 326\left(m_{4}\right)$ is the ratelimiting process for the overall rotary step characterized by the I $\rightarrow \mathrm{F}$ transition. The interaction strengths between the six Rho subunits and the RNA residues in states I, IM1, IM2, and F are shown in Figure S4. Interestingly, discrete transitions of side chain conformations are also seen in the case of myosin whose recovery stroke involves side chain motions activated between a few discrete states as reported by Elber et al. ${ }^{41}$

To inspect along the I $\rightarrow$ F transition overall RNA translocation and Rho conformational change, the latter property was characterized for this purpose through $\triangle$ RSMD $=\operatorname{RSMD}(\mathrm{Y}, \mathrm{I})-\operatorname{RSMD}(\mathrm{Y}, \mathrm{F}))^{42}$ here $\operatorname{RSMD}(\mathrm{Y}, \mathrm{Z})$ is the
conformational RMSD difference between two conformations $Y$ and $Z$ ( $Z$ in state $I$ or $F$ ). The free energy landscape presented in Figure 5 reveals an RNA translocation distance of


Figure 5. Free energy landscape for RNA translocation distance and Rho conformation for $\mathrm{X}=\mathrm{E}$. The energy values are defined by the color bar in units of $\mathrm{kcal} / \mathrm{mol}$. States I, IM1, IM2, and F are labeled with black dots. The RNA translocation distance is defined as the center of mass distance between RNA backbone (residues 3-8) and Rho backbone (C-terminal domain). The Rho conformational coordinate is defined in the text.
about $2.4 \AA$ in going from states I to F, which is commensurate with the helical rise per base pair seen in the Rho-RNA complex; $\triangle \mathrm{RSMD}$ varies from -4 to $4 \AA$ in going from states I to F , implying that the full conformational change is necessary in realizing the RNA translocation. For comparison, we present in Figure S5 the free energy map for the unreleased product case $\mathrm{X}=\mathrm{D}$ (see Figure 2c), which shows transition from a stable state I to a very unstable state F, clearly an unfavorable process.

Extension from a Single Rotary Reaction Step to Multiple Steps. The scenario described above for one rotary reaction step can be readily extended to an arbitrary number of such steps. ${ }^{9}$ As shown in Table S4 the step 1 hexatuples of ligand states ( $\mathrm{T} * \mathrm{~T} * \mathrm{TTED} \rightarrow \mathrm{DT} * \mathrm{~T} * \mathrm{TTE}$ ) corresponding to the transition $\mathrm{R} \rightarrow \mathrm{F}$ can be continued by shifting the step 1 ligand states by one Rho subunit. Table S4 provides the detailed ligand states for step $2,3, \ldots 7$, where step 7 exhibits again the same ligand states as step 1 ; the shifts complete in step 6 a full cycle $\left(360^{\circ}\right)$ through all six Rho subunits. For example, step 2 involves then ligand state changes $\mathrm{DT}^{*} \mathrm{~T} * \mathrm{TTE}$ $\rightarrow$ EDT*T*TT; step 7 involves ligand state changes T*T*TTED $\rightarrow$ DT*T*TTE. The RNA translocation in a full cycle (six steps) is illustrated in Movie S1, while Movie S2 shows the relative motion of six Rho subunits in a full cycle. The reader is urged to view both videos for better comprehension of the simulation results.

Allosteric Pathway That Couples RNA Translocation to Hydrolysis Product Release. RNA translocation after step 1 requires at the beginning of step 2 the release of hydrolysis product $\mathrm{ADP}+\mathrm{Pi}$ at the $m_{1} / m_{2}$ interface. In fact, when we assumed for step 1 that the respective release of "old" product at the $m_{6} / m_{1}$ interface does not take place, the rotatory reaction step is endergonic and cannot proceed (see case $\mathrm{X}=\mathrm{D}$ in Figure 2c). Likewise, for step 2, the hydrolysis product at the $m_{1} / m_{2}$ interface must be released before the next step of RNA translocation can proceed. For this purpose the hydrolysis product at the $m_{1} / m_{2}$ interface, which we termed "new" product, must experience a change from being tightly bound (D* state, see Figure 2a) to being loosely bound (D state) and, therefore, ready for subsequent release. One may hypothesize
then that the initiation of step 2 in the form of a $D \rightarrow E$ transition at the $m_{1} / m_{2}$ interface during the next dwell phase should actually be prepared when state $F$ is reached in step 1 . It appears that such lockstep synchronization is indeed achieved by Rho through an allosteric pathway that links disengagement of K326 ( $m_{1}$ ) from RNA backbone phosphate $\mathrm{P}_{3}$ (see Figure 4) to a liberation of inorganic phosphate Pi from a salt bridge with R269 $\left(m_{1}\right)$. This liberation looses the binding of Pi; we show below that the nearby ADP moiety becomes also more flexible.

We discovered the allosteric pathway by monitoring the interaction energy deviation along the simulated pathway between residue $s$ of Rho and all residues of neighboring subunits, $\Delta E_{s}^{\text {subunit-subunit }}$ (see SI text and Figure S6b). The larger $\Delta E_{s}^{\text {subunit-subunit }}$ is, the more important contribution residue $s$ will make to the relative stability of different states along the pathway. Such residues $s$, namely those with $\Delta E_{s}^{\text {subunit-subunit }}>5 \mathrm{kcal} / \mathrm{mol}$, are listed in Table S3. Among the residues listed, R272 $\left(m_{1}\right)$, E333 $\left(m_{2}\right)$, E334 $\left(m_{2}\right)$, and R269 ( $m_{1}$ ) participate in the stated allosteric coupling between RNA and Pi. The corresponding pathway is illustrated in Figure 6.

The suggested allosteric mechanism at the $m_{1} / m_{2}$ interface (i.e., the interface involved in the $\mathrm{T}^{*} \rightarrow \mathrm{D}^{*} \rightarrow \mathrm{D}$ transition) is seen clearly when one follows the conformations of residues R272 $\left(m_{1}\right)$, $\mathrm{E} 333\left(m_{2}\right)$, $\mathrm{E} 334\left(m_{2}\right)$, and R269 $\left(m_{1}\right)$ during the I $\rightarrow$ IM1 $\rightarrow$ IM2 $\rightarrow \mathrm{F}$ transitions in Figure 6a-d. One can recognize that $\mathrm{K} 326\left(m_{1}\right)$ disengages from $\mathrm{P}_{3}$ of RNA during


Figure 6. Allosteric coupling between RNA translocation and Pi of the hydrolysis product. The coupling is established through a link between the disengagement of $\operatorname{K326}\left(m_{1}\right)$ from RNA phosphate $\mathrm{P}_{3}$ and release of Pi from a salt bridge with R269 $\left(m_{1}\right)$. The figure shows in ( $\mathrm{a}, \mathrm{b}, \mathrm{c}, \mathrm{d}$ corresponding to states I, IM1, IM2, F, respectively) top-down views (same view of Rho as in Figure 1a) the conformational changes of residues $\operatorname{R272}\left(m_{1}\right), \operatorname{E333}\left(m_{2}\right), \operatorname{E334}\left(m_{2}\right)$, and $\operatorname{R269}\left(m_{1}\right)$ at the $m_{1} / m_{2}$ interface during transitions I $\rightarrow$ IM1 $\rightarrow$ IM2 $\rightarrow$ F. The three transitions are shown as black arrows; red arrows indicate large side chain movements occurring before the next transition takes place. RNA is shown as a pink ribbon with phosphate $P_{3}$ highlighted as a $\tan$ sphere.
the initial I $\rightarrow$ IM1 transition (Figures 6a,b and 4b); the disengagement triggers a downward motion of $m_{1}$ (Figure 3a). During the IM1 $\rightarrow$ IM2 transition, E333 $\left(m_{2}\right)$ forms a contact with R272 $\left(m_{1}\right)$ during the sliding motion between subunits $m_{1}$ and $m_{2}$ (Figure 3a). In the final transition $\mathrm{IM} 2 \rightarrow \mathrm{~F}, \operatorname{S325}\left(m_{1}\right)$, on the same R loop as $\mathrm{K} 326\left(m_{1}\right)$, engages $\mathrm{R} 272\left(m_{1}\right)$. Meanwhile the salt bridge network at the $m_{1} / m_{2}$ interface further adjusts its configuration: R272 $\left(m_{1}\right)$, which is coordinated with $\mathrm{E} 334\left(m_{2}\right)$ in state IM2, establishes a firm contact with E333 $\left(m_{2}\right)$ in state F, and R269 $\left(m_{1}\right)$ disengages from Pi and forms a salt bridge with E334 $\left(m_{2}\right)$, weakening its interactions with Pi considerably. As a result, Pi becomes weakly bound at the very end of step 1 .

Comparing trajectories (carried out in Voronoi cells as described in the Methods section) at the beginning (state I) and the end (state F) of the motor-action phase shows that along with the loosening of Pi binding also the ADP moiety bound at the $m_{1} / m_{2}$ interface becomes more loosely bound as reflected in its position deviation shown in Figure S10. The average deviation changes from 0.6 to $1.4 \AA$, illustrating that the ADP molecule upon the I $\rightarrow \mathrm{F}$ transition along with Pi becomes loosely bound and ready for release.

## DISCUSSION AND CONCLUSION

The present study investigated through MD simulations how the homohexamer Rho translocates RNA during the ATP hydrolysis cycle. The modeling is based on the important crystallographic structure ${ }^{9}$ that showed the identical and circularly arranged Rho subunits $m_{1}, m_{2}, \ldots, m_{6}$ with the hexameric symmetry broken through adoption of an asymmetric pattern of six ligand states. The result of the MD simulations going beyond the stated structure is the actual detailed conformational transition pathway of the Rho-RNA complex via four key states (I, IM1, IM2, F), along with the associated free energy, kinetic information, and, in particular, the coupling and synchronization between Rho's ligand state changes and RNA translocation.

The all-atom millisecond dynamics of the Rho-RNA complex describes the force-generation mechanism for Rho in unprecedented detail and applies likely to other hexameric ring-type ATPase motors. As shown in Figure S1, Rho dynamics involves a dwell phase in which ATP binding, release of "old" product and ATP hydrolysis into "new" product take place and a motor-action phase ( $\mathrm{I} \rightarrow \mathrm{F}$ ). The rate-limiting release of "old" product ends the dwell phase and triggers the motor-action phase, as demonstrated in Figure 2. The dynamics underlying RNA translocation during the motor-action phase involves highly coordinated translational and rotational movements of the six subunits in the Rho ring, but not internal motion of the individual subunits. The force-generation process, linked to the crossing of the major free energy barrier along the $\mathrm{I} \rightarrow \mathrm{F}$ transition, is actually associated with the disengagement of K326 of the leading subunit (the top position of the six K326 residues arranged in a spiral staircase) from an RNA phosphate; the barrier crossing corresponds to the $107 \mu \mathrm{~s}$ slow IM1 $\rightarrow$ IM2 transition. A non-native interaction between the side chain of K326 and an RNA base appears at the state IM1, suggesting sequence-dependent activity of Rho. ${ }^{43}$

The directionality of RNA translocation is determined by the interaction pattern between the RNA backbone and the ringshaped motor as well as the direction of the rotary ATP hydrolysis cycle along the ring. ${ }^{1}$ We found that the forward R $\rightarrow \mathrm{F}$ reaction is triggered by release of "old" hydrolysis product;
the reverse rotary reactions $\mathrm{F} \rightarrow \mathrm{I}$ and $\mathrm{I} \rightarrow \mathrm{R}$ are highly unfavorable, since the former step is endergonic (Figure 2b) and the later step is extremely hard to happen due to irreversibility of ADP/Pi release and ATP hydrolysis. ${ }^{19,20}$ Upon completion of ligand state changes in a rotary reaction step, both conformational states (I and F) exist; however only state F is ready for ligand state changes in the next step. For example, as the simulations revealed, RNA translocation is allosterically coupled to loosening the binding of the "new" hydrolysis product, initially in state $\mathrm{D}^{*}$ and transitioning to state D , such that product is ready to be released in the subsequent dwell phase.

Due to the large number of residues involved in the transition pathway, we had to apply in the present study a statistical analysis to capture the residues that make significant contributions to the changes in the subunit-subunit interaction energy along the transition pathway. These residues exert their influence on the relative stability of different conformational states as well as on the friction ${ }^{44}$ at interfaces between subunits. For example, a salt bridge, R272-E333, stabilizes the state IM2; another salt bridge, R269-E334, stabilizes the state F. Among the list of identified residues (listed in Tables S2 and S3) about half of the residues are connected with mutations that have been demonstrated already in respective experiments to lead to functional deficiencies, including residues K326, R272, E333, E334, R269 and other allosteric residues as reported in refs 43 and 45-48; the remaining listed residues, not tested yet in mutagenesis studies, are good candidates for future experiments that further explore the structure-function relationship of Rho. The electrostatic nature of the allosteric pathway increases the friction at interfaces ${ }^{44}$ and slows down the motor dynamics to a millisecond time scale.

The rotary reaction step investigated here is also found in other hexameric motors. Crystal structures of bovine papillomavirus E1 and Bacillus stearothermophilus DnaB hexameric helicase reveal asymmetric functional states in the ATPase cycle (like the prior R state in Figure 1). E1 is proposed to translocate one nucleotide of ssDNA every rotary reaction step; ${ }^{8}$ the nonplanar DnaB structure indicates that DnaB can translocate two nucleotides of ssDNA per rotary reaction step, given that each subunit of DnaB accommodates two nucleotides. ${ }^{10}$
$\mathrm{F}_{1}-/ \mathrm{V}_{1}$-ATPases share an evolutionary link with, and are homologous to, Rho. ${ }^{18,49,50}$ We note that the sequences of the ATPase domain of $\mathrm{F}_{1}-/ \mathrm{V}_{1^{1}}$-ATPases are about 50-100 aa longer than the ATPase domain of Rho; the additional 50-100 aa residues form a C-terminal domain that can swing relative to a central domain of F1-/V1-ATPases. Such a feature is important for rotating their central stalks instead of moving substrate linearly. Though carrying out a very different function, $\mathrm{F}_{1^{-}} / \mathrm{V}_{1^{-}}$ ATPase and Rho share similarities in their ATPase cycle. Single-molecule and biochemical studies ${ }^{51,52}$ show that $\mathrm{V}_{1^{-}}$ ATPase pauses its central stalk every $120^{\circ}$ without any submillisecond substeps, similar to the rotary step of $60^{\circ}$ in the case of Rho. Recently, a series of intermediate structures of Enterococcus hirae $\mathrm{V}_{1}$-ATPase were reported, ${ }^{12,53}$ suggesting a pathway of a rotary reaction step: after ATP hydrolysis, ADP/Pi release is the rate-limiting process that would induce the $120^{\circ}$ central stalk rotation (ATP binding is relatively fast); as a result of the stalk rotation, the prior ATP bound interface will change from state T to state $\mathrm{T}^{*}$. The Rho transition pathway shows similarities with the rotary reaction step in $\mathrm{V}_{1}$-ATPase: ATP hydrolysis, ATP binding, and ADP/Pi release take place during

Rho's dwell phase before they trigger RNA translocation. As the main barrier crossing event for RNA translocation happens at the IM1 $\rightarrow$ IM2 stage (as demonstrated in Figures 4a and 5), the $\mathrm{T} \rightarrow \mathrm{T}^{*}$ transition (documented in Figures S8-S9), which occurs during the IM2 $\rightarrow \mathrm{F}$ stage, is preceded by RNA translocation.

The coordination of catalytic processes at the subunit interfaces is important for hexameric motors' function. ${ }^{2}$ The central stalk rotation of Escherichia coli $\mathrm{F}_{1}$-ATPase, repeated in $120^{\circ}$ steps, involves two substeps. ${ }^{54,55}$ In each of the $120^{\circ}$ steps, ATP binding, ATP hydrolysis, and product release processes are separated into two dwell phases, namely a first binding dwell before a $80^{\circ}$ subrotation and a second catalytic dwell before a $40^{\circ}$ subrotation. However, for $\mathrm{V}_{1}$-ATPase and Rho, there are no substeps, and thus the three catalytic processes all happen before the hexameric motors carry out work (see Figure S1). The timing of when catalytic processes are ready to take place is controlled by the conformational transitions of the motors. Once the corresponding interfaces are competent to carry out the respective reactions, the reactions occur stochastically with first-order kinetics whose rates are determined by the local binding sites. ${ }^{29,56}$ Four key transitions were observed in our simulations: (1) the allosteric regulation at the $m_{1} / m_{2}$ interface ( $\mathrm{D}^{*} \rightarrow \mathrm{D}$ ) renders ADP + Pi competent to be released; (2) the $m_{6} / m_{1}$ interface opening renders the interface capable of binding a new ATP molecule; (3) the ATP binding transition at the $m_{5} / m_{6}$ interface (Figure S7) moves the ATP into the binding pocket; (4) the transition $\mathrm{T} \rightarrow \mathrm{T}^{*}$ at the $m_{3} / m_{4}$ interface (Figures S8, S9) renders ATP competent to be hydrolyzed. In our simulations, we observed the ordering of transitions, namely (3) $\rightarrow$ (2) $\rightarrow$ (1), (4).

Recent single-molecule fluorescence studies have provided unprecedented insight into the dynamic unwinding processes of hexameric helicases. A recent single-molecule fluorescence study of T7 gp4 hexameric helicase, ${ }^{57}$ together with a highresolution measurement on the chemical step size of T7, ${ }^{58}$ suggests that the ratio between number of nucleotides hydrolyzed and number of bp unwound is $1: 1$. However, for G-C base-pairs, the unwinding signal shows stochastic pauses every $2-3 \mathrm{bp}$, implying $2-3 \mathrm{bp}$ are unwound after enough elastic energy is stored when 2-3 ATP got hydrolyzed. For A-T base-pairs, a sequential reaction mechanism with 1 bp step size is proposed, similar to the case of the present study. Thus, the free energy landscape of conformational transitions during rotary steps needs to be adapted to accommodate different types of nucleotide substrates. Nevertheless, the free energy release of Rho during its $\mathrm{I} \rightarrow \mathrm{F}$ transition, $G_{\mathrm{I}}-G_{\mathrm{F}}$, is $1.5 \mathrm{kcal} /$ mol, comparable to the $\sim 1 \mathrm{kcal} / \mathrm{mol}(\mathrm{A}-\mathrm{T})$ or $\sim 2 \mathrm{kcal} / \mathrm{mol}$ (CG) base-paring free energy. ${ }^{59}$ The molecular basis for unwinding by hexameric helicase, unfolding by proteasome, and stalk rotation by $\mathrm{F}_{1}-/ \mathrm{V}_{1}$-ATPases can be explored in future studies following the computational approach employed in the present study.

## METHODS

Here we describe first the molecular modeling of the hexameric helicase Rho and the procedures used for the MD simulations. Then, we introduce the string method ${ }^{35}$ that we apply to calculate the most probable transition path (MPTP). ${ }^{35,60}$ Finally, we outline how the milestoning method ${ }^{37,39,61}$ allowed us to calculate free energy and kinetics along the Rho-RNA transition pathway. We note that the total simulation time, including string method calculation and enhanced sampling for free energy and kinetics, adds up to $\sim 10 \mu$ s and involves $\sim 0.4$ million atoms.

Molecular Modeling and Simulation Setup. Our MD study is based on a crystal structure of Rho loaded with RNA (six uracil nucleobases) from E. coli (pdb code: 3ICE; see Figure 1). In our simulations we replaced the ATP-mimics ( $\mathrm{ADP} \cdot \mathrm{BeF}_{3}$ ) in the crystal structure by the equivalent ATP molecules in the $\mathrm{T}^{*}$ and T states, introduced an ADP and an inorganic phosphate (modeled as $\left.\mathrm{H}_{2} \mathrm{PO}_{4}^{-}\right)^{62}$ in case of the D state, and removed the loosely bound ATP-mimic in the E state. Structural analyses ${ }^{63,64}$ have demonstrated that nonhydrolyzable $\mathrm{ADP} \cdot \mathrm{BeF}_{3}$ can successfully mimic the ATP and ADP-Pi binding states in $\mathrm{F}_{1}$-ATPase; different ATP analogues produce actually similar binding conformations. We also added to the six uracil nucleobases of the RNA in the structure three uracil nucleobases to the $3^{\prime}$ end, such that the simulated system contained RNA with nine uracil nucleobases. We denote by $\mathrm{P}_{j}$ the RNA backbone phosphate groups and by $U_{j}$ the nucleobase of the RNA residue for $j=1, \ldots, 9$.

The protein-ligand-RNA system was solvated in a $120 \times 170 \times 170$ $\AA^{3}$ water box with 150 mM NaCl ; the simulated system involved altogether $\sim 0.36$ million atoms. After a 4000 -step energy minimization, the system was heated in the NPT ensemble ( 1 atm ) to 300 K in 50 ps , employing harmonic constraints with $1 \mathrm{kcal} /\left(\mathrm{mol} \AA^{2}\right)$ spring constant to the heavy atoms. Keeping the spring constant, a 1 ns equilibration in the NPT ensemble ( 1 atm at 300 K ) was carried out, followed by a 4 ns NVT ensemble simulation, gradually decreasing the spring constant to zero during the latter stage. In the following, we refer to the state of the resulting protein-RNA system as the prior state R (see Figure 1b). All MD simulations in our study were performed using NAMD $2.9^{65}$ with the CHARMM27 force field and CMAP corrections.

The aim of our study is to identify the mechanism of an elementary propagation step of Rho. The step involves a prior state R and a final state F that are to be linked through a conformational transition. As the actual propagation ( $\mathrm{R} \rightarrow \mathrm{F}$ ) occurs typically on a millisecond time scale, straightforward MD simulation cannot simulate this transition, and enhanced conformational sampling based on a so-called string method is employed instead. In the present case the hexameric symmetry of Rho dictates that F , in principle, is identical to R with all subunits shifted by one. To construct F one needs to permute the geometries of $S_{1}(R), S_{2}(R), \ldots, S_{6}(R)$, where $S_{j}(R)\left[S_{j}(F)\right]$ denotes the geometry of subunit $j$ in Rho state R [state F ] as follows: $\mathrm{S}_{1}(\mathrm{~F})=$ $S_{6}(R), S_{2}(F)=S_{1}(R), \ldots, S_{6}(F)=S_{5}(R)$.

We introduce an initial state I (see Figure 2a) between R and F. State I represents a state of Rho, in which ATP hydrolysis and new ATP binding in the prior state $R$ have just taken place such that Rho is driven to a new geometry of its subunits, namely the one corresponding to state F. In other words, I represents a state energized through changes in ligand binding states. I is constructed from the prior state R as follows: at the $m_{1} / m_{2}$ interface one hydrolyzes one ATP molecule by superimposing an ADP and Pi onto the ATP position ( $\mathrm{T}^{*} \rightarrow \mathrm{D}^{*} ; \mathrm{D}^{*}$ denotes the state of "new" product that presumably is more tightly bound than "old" product in state D ); at the $m_{5} / m_{6}$ interface one docks one incoming ATP molecule into the loosely bound ATP-mimic position ( $\mathrm{E} \rightarrow \mathrm{T}^{-}$; $\mathrm{T}^{-}$represents a state with a loosely bound ATP); at the $m_{1} / m_{6}$ interface, we actually adopt two alternatives for the ligand state, referring to either state as X : in the first case, referred to as $\mathrm{X}=\mathrm{E}$, we removed $\mathrm{ADP} / \mathrm{Pi}(\mathrm{D} \rightarrow \mathrm{E})$, and in the second case, referred to as $\mathrm{X}=\mathrm{D}$, we left $\mathrm{ADP} / \mathrm{Pi}$ unchanged in the pocket; the other three ligand states remain unchanged at the $m_{2} /$ $m_{3}$ interface ( $\mathrm{T}^{*}$ ), $m_{3} / m_{4}$ interface ( T ), and $m_{4} / m_{5}$ interface (T).

The resulting state I system was then equilibrated for 30 ns , and the final snapshot was taken as the initial state I. To compare the conformational changes between state I and the crystal structure, binding pocket $\mathrm{C}_{\alpha}$ RMSDs of subunits are listed in Table S5; the RMSD values listed are small, indicating that the nonhydrolyzable $\mathrm{ADP} \cdot \mathrm{BeF}_{3}$ employed in the crystal structure has binding conformations that are very similar to those of ATP/ADP•Pi molecules employed in our simulations and in functional Rho.

The modeling of I adopted in the present study is justified for the following reasons. First, the time scale for ATP hydrolysis estimated from experiments to be 1 ms (ref 20) or 6.7 ms (ref 19) is shorter than the rate-limiting time for ADP release ( 10 ms , ref 20 ) or Pi release ( 20
ms, ref 19). As R resembles the catalytic dwell structure (the crystal structure ${ }^{9}$ was obtained while binding to Rho a nonhydrolyzable ATP analogue), ATP hydrolysis in R will necessarily precede the conformational transition toward F. Second, for the metabolite concentration of ATP in E. coli $(\sim 10 \mathrm{mM})^{66}$ the time scale for ATP binding is $<0.5 \mathrm{~ms}$ (refs 19 and 20), which is much shorter than the time scales of the other two processes (ATP hydrolysis and product release). Thus, one ATP molecule will very likely diffuse to the E (empty) site of R and become weakly bound in $\mathrm{I}\left(\mathrm{E} \rightarrow \mathrm{T}^{-}\right.$at the $m_{5} /$ $m_{6}$ interface) before the other two ligand processes take place. In the simulation, we have four ATP bound in R. Since each Rho hexamer accommodates around 3.5 ATP on average under saturating conditions, ${ }^{19}$ one ATP hydrolysis reaction ( $\mathrm{T}^{*} \rightarrow \mathrm{D}^{*}$ ), namely the one at the $m_{1} / m_{2}$ interface in state I, will keep a suitable number of ATP molecules bound in Rho. Whether product release process is important to trigger the conformational transition is explored by simulations assigning for state X either state E or state D .

String Method Protocol. In the present study we opted for the so-called "string method with swarms-of-trajectories"35 to describe the roughly millisecond-scale I $\rightarrow \mathrm{F}$ transition pathway which is represented by a "string" in a space of "collective variables" $z(x), z$ being $n$-dimensional functions of Cartesian coordinates $x$ of the system $\left(x \in \mathbb{R}^{3 N}\right)$. The string is discretized into $M+1$ equally spaced images, which are conformational states of Rho along the $\mathrm{I} \rightarrow \mathrm{F}$ transition and are characterized by the set of collective variables $z^{(0)}, z^{(1)}, \ldots, z^{(M)}$ (here $M=50$ ). A swarm of short trajectories ( 4 ps ) is launched for each image, and the image evolves according to the average drift of its trajectory swarm during one iteration. The pathway is then optimized iteratively until it converges to the most probable transition path.

Due to the high dimensionality of the movement in the $\mathrm{I} \rightarrow \mathrm{F}$ transition, we needed to modify the string method protocol introduced in ref 35 . On the one hand, we had to select $z$ through a systematic computational procedure as the large number of collective variables needed could not be hand-picked (Rho has altogether $\sim 40,000$ atoms); on the other hand we had to employ multidimensional curve fitting, as used previously in simulation studies, ${ }^{67,68}$ in order to reduce the noise arising from a thermal multidimensional system, appearing here in the form of noisy kinks in the transition pathway (string). The collective variables suitable for the present case should describe the dominant changes that arise during the $\mathrm{I} \rightarrow \mathrm{F}$ transition. These collective variables were identified to be the positions of key residues at the six subunit-subunit interfaces of the hexamer. We determined the residue-based interaction energy contribution of Rho subunits as shown in Figure S2b, the energy serving as a collective variable selection criterion as explained in Supporting Information. From this procedure resulted eventually $660 \times 3=1980$ coordinate positions.

Our implementation of the string method benefitted from a scalable multiple copy algorithm ${ }^{69}$ which enables launching thousands of trajectories simultaneously on a petascale supercomputer. The total simulation time needed for the sum of all string method trajectories amounted to $8 \mu \mathrm{~s}$ for the two pathways depicted in Figure 2. More details of our protocol, including choice of collective variables, generation of initial configurations, evolution of the string, and convergence of the final pathway are provided in Supporting Information.

Free Energy and Kinetics Calculations. In order to compute the free energy profile along the two I $\rightarrow$ F transition pathways for $\mathrm{X}=\mathrm{E}$ and $\mathrm{X}=\mathrm{D}$ we employed the enhanced sampling method described in refs 39,61 . For this purpose we applied a Voronoi tessellation ${ }^{39}$ in the collective variable space with $M=51$ cells, whose centroids are the images $z^{\{\alpha\}}$ of the converged transition path. The points $z(x)$ assigned to a Voronoi cell $B_{i}$ are characterized through the Voronoi tessellation rule (eq S8, Supporting Information). In order to enhance the sampling, 20 conventional 0.8 ns -long MD simulations were carried out in each Voronoi cell with random seed employing reflective boundaries at the cell interfaces. The implementation details of the sampling along with the calculation of the equilibrium probability $\pi_{i}$ and free energy $G_{i}$ for the system in cell $B_{i}$ can be found in Supporting Information (eqs S9-S11).

Through the milestoning method developed in refs 37,39 , and 61 , the MFPTs for traversing from state I to state F can be computed. The kinetic rates predicted by milestoning have been shown to be comparable to experimental values. ${ }^{41,70}$ In milestoning, ${ }^{36,37}$ instead of performing a long-time MD trajectory, the transition event is split into short trajectories crossing a set of "milestones" (hypersurfaces) along the pathway between the initial and final states. Here the interfaces of Voronoi cells $B_{i}$ and $B_{j}$ are chosen as milestones, labeled by indices 0 , $1, \ldots, N_{T}\left(N_{T} \neq M\right)$. Statistical properties of crossing the set of milestones are utilized to reconstruct the information on the transition rates; the rate matrix $\mathbf{q}_{i j}$ of instantaneous transition from milestone $i$ to milestone $j$ is obtained by eq $S 13^{39,61}$ in Supporting Information and is based on the confined simulations within the Voronoi cells introduced above. The MFPTs from milestone $m$ to milestone $n, \tau_{m, n}$, can be then obtained by solving the system of $N_{T}$ linear equations: ${ }^{37,39,61,71}$

$$
\sum_{\substack{m=0 \\ m \neq n}}^{N_{T}} \mathbf{q}_{k m} \tau_{m, n}=-1, \quad k \neq n
$$

The sampling inside all Voronoi cells required a total simulation time of $1.6 \mu \mathrm{~s}$ for two free energy profiles and associated MFPTs between states I and F along the reaction coordinate in Figures 2b,c $(0.8 \mu \mathrm{~s}$ each).

## - ASSOCIATED CONTENT

## (S) Supporting Information

A schematic figure showing dwell and RNA-translocation phases of Rho dynamics; details of computational methods; additional information on the analysis of interaction between Rho and RNA; residue-based interaction energy scanning and predicted important residues; supporting description of key residues involved in ATP binding transitions; and Movies S1 and S2. This material is available free of charge via the Internet at http://pubs.acs.org.

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## Notes

The authors declare no competing financial interest.

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